

COMPLEX ANALYSIS AND SPECIAL FUNCTIONS

| IV Semester: ECE | | | | | | | | |
|--|------------|-----------------------------|---|-------------------------------|---------|---------------|--------------------------|-------|
| Course Code | Category | Hours / Week | | | Credits | Maximum Marks | | |
| AHSC12 | Foundation | L | T | P | C | CIA | SEE | Total |
| | | 3 | 1 | 0 | 4 | 40 | 60 | 100 |
| Contact Classes: 45 | | Tutorial Classes: 15 | | Practical Classes: Nil | | | Total Classes: 60 | |
| Prerequisite: Basic Principles of complex functions | | | | | | | | |
| I. COURSEOVERVIEW: | | | | | | | | |
| <p>This course Complex Analysis and Special Functions provides an introduction to complex analysis which is theory of complex functions with complex variable. The course includes complex functions and differentiation, complex integration, power series expansion of complex function and special functions. The mathematical skills derived from this course form a necessary base to analytical and design concepts encountered in the program.</p> | | | | | | | | |
| II. COURSE OBJECTIVES: | | | | | | | | |
| The course will enable the students to learn: | | | | | | | | |
| <ol style="list-style-type: none"> I. The applications of complex variable and conformal mapping in two dimensional complex potential theories. II. The fundamental calculus theorems and criteria for the independent path on contour integral used in problems of engineering. III. The concepts of special functions and its application for solving the partial differential equations in physics and engineering. IV. The mathematics of combinatorial enumeration by using generating functions and complex analysis for understanding the numerical growth rates. | | | | | | | | |
| III. COURSE SYLLABUS: | | | | | | | | |
| MODULE-I COMPLEX FUNCTIONS AND DIFFERENTIATION (09) | | | | | | | | |
| Complex functions differentiation and integration: Complex functions and its representation on argand plane, concepts of limit, continuity, differentiability, analyticity, Cauchy-Riemann conditions and harmonic functions; Milne-Thomson method. Bilinear Transformation. | | | | | | | | |
| MODULE -II COMPLEX INTEGRATION (09) | | | | | | | | |
| Line integral: Evaluation along a path and by indefinite integration; Cauchy's integral theorem; Cauchy's integral formula; Generalized integral formula; Power series expansions of complex functions and contour Integration: Radius of convergence. | | | | | | | | |
| MODULE -III POWER SERIES EXPANSION OF COMPLEX FUNCTION (09) | | | | | | | | |
| Expansion in Taylor's series, Maclaurin's series and Laurent series. Singular point; Isolated singular point; Pole of order m; Essential singularity; Residue: Cauchy Residue Theorem. | | | | | | | | |
| Evaluation of Residue by Laurent Series and Residue Theorem. | | | | | | | | |
| Evaluation of integrals of the type $\int_0^{2\pi} f(\cos\theta, \sin\theta)d\theta, \int_{-\infty}^{\infty} f(x)dx$ | | | | | | | | |
| MODULE -IV SPECIAL FUNCTIONS-I (09) | | | | | | | | |
| Improper integrals; Beta and Gamma functions: Definitions; Properties of Beta and Gamma function; Standard forms of Beta functions; Relationship between Beta and Gamma functions. | | | | | | | | |
| MODULE -V SPECIAL FUNCTIONS-II (09) | | | | | | | | |
| Bessel's Differential equation: Bessel function, properties of Bessel function, Recurrence relations of Bessel function, Generating function and Orthogonality of Bessel function, Trigonometric expansions involving Besse function. | | | | | | | | |

IV. TEXT BOOKS

1. Kreyszig, "Advanced Engineering Mathematics", John Wiley & Sons Publishers, 10th Edition, 2010.
2. B. S. Grewal, "Higher Engineering Mathematics", Khanna Publishers, 43rd Edition, 2015.

V. REFERENCE BOOKS:

1. T.K.V Iyengar, B.Krishna Gandhi, "Engineering Mathematics - III", S.Chand& Co., 12th Edition, 2015.
2. RK Jain & SRK Iyengar, "Advanced Engineering Mathematics", Narosa Publishers, 5th Edition, 2016.

VI. WEB REFERENCES:

1. http://www.efunda.com/math/math_home/math.cfm
2. <http://www.ocw.mit.edu/resourcs/#Mathematics>
3. <http://www.sosmath.com>
4. <http://www.mathworld.wolfram.com>

VII. E-TEXT BOOKS:

1. <http://www.keralatechnologicaluniversity.blogspot.in/2015/06/erwin-kreyszig-advanced-engineering-mathematics-ktu-ebook-download.html>
2. <http://www.faadooengineers.com/threads/13449-Engineering-Maths-II-eBooks>